

Chapter 1: Binary Systems

Solutions of Problems: [2, 5, 8, 16, 18, 21, 31, 34]

Problem: 1-2

What is the exact number of bytes in a system that contains (a) 32 Kbyte, (b) 64 M bytes, and (c) 6.4 Gbyte?

Solution:

The exact number of bytes in a system that contains

(a) 32K byte = 32×2^{10} byte = 32,768 byte

(b) 64M bytes = 64×2^{20} bytes = 67,108,864 bytes

(c) 6.4G byte = 6.4×2^{30} byte = 6,871,947,674 byte

Problem: 1-5

Determine the base of the numbers in each case for the following operations to be correct:

(a) $14/2 = 5$ (b) $54/4 = 13$ (c) $24+17=40$

Solution:

The base of the numbers in each case for the following operations to be correct:

(a) $14/2 = 5$;

Find decimal equivalent

$$14 = 1 \times r^1 + 4 \times r^0 = r + 4$$

$$2 = 2 \times r^0 = 2$$

$$5 = 5 \times r^0 = 5$$

$$(4+r)/2=5$$

Solving this equation, we get $r=6$, base 6

(b) $54/4 = 13$;

Find decimal equivalent

$$54 = 5 \times r^1 + 4 \times r^0 = 5r + 4$$

$$4 = 4 \times r^0 = 4$$

$$13 = 1 \times r^1 + 3 \times r^0 = r + 3$$

$$(5r+4)/4 = r + 3$$

Solving this equation, we get $r=8$, base 8

(c) $24+17=40$;

Find decimal equivalent

$$24 = 2 \times r^1 + 4 \times r^0 = 2r + 4$$

$$17 = 1 \times r^1 + 7 \times r^0 = r + 7$$

$$40 = 4 \times r^1 + 0 \times r^0 = 4r + 0$$

$$(2r + 4) + (r + 7) = 4r$$

Solving this equation, we get $r=11$, base 11

Problem: 1-8

Convert the following binary numbers to hexadecimal and to decimal:

a) 1.11010, b) 1110.10

Explain why the decimal answer in (b) is 8 times that of (a).

Solution:

To convert from binary to hexadecimal:

Each 4 binary digits is equal to 1 hexadecimal digit:

$$\text{a) } (1.11010)_2 = (1.D0)_{16}$$

$$\text{b) } (1110.10)_2 = (E.8)_{16}$$

To convert from binary to decimal:

$$\text{a) } (1.11010)_2 = (1.8125)_{10}$$

$$1 \times 2^0 + 1 \times 2^{-1} + 1 \times 2^{-2} + 0 \times 2^{-3} + 1 \times 2^{-4} + 0 \times 2^{-5} = (1).(0.5+0.25+0.0625)$$

$$\text{b) } (1110.10)_2 = (14.5)_{10}$$

$$1 \times 2^3 + 1 \times 2^2 + 1 \times 2^1 + 0 \times 2^0 + 1 \times 2^{-1} + 0 \times 2^{-2} = (8+4+2).(0.5)$$

The decimal answer in (b) is 8 times that of (a) because the binary number in (b) is the same as that in (a) except that the point is shifted to the right 3 digits and this means that it is multiplied by 2^3 .

Problem: 1-16

Obtain the 1's and 2's complement of the following binary numbers:

a) 11101010 b) 01111110 c) 00000001 d) 10000000 e) 00000000

Solution:

1's complement : change every 1 to 0 and vice versa.

2's complement : change every 1 to 0 and vice versa ,then add (1) to the least significant bit.

$$\text{a) } \begin{array}{l} 11101010 \\ 1's \text{ complement : } 00010101 \\ 2's \text{ complement : } 00010110 \end{array}$$

$$\text{b) } \begin{array}{l} 01111110 \\ 1's \text{ complement : } 10000001 \\ 2's \text{ complement : } 10000010 \end{array}$$

$$\text{c) } \begin{array}{l} 00000001 \\ 1's \text{ complement : } 01111110 \\ 2's \text{ complement : } 11111111 \end{array}$$

$$\text{d) } \begin{array}{l} 10000000 \\ 1's \text{ complement : } 01111111 \\ 2's \text{ complement : } 10000000 \end{array}$$

$$\text{e) } \begin{array}{l} 00000000 \\ 1's \text{ complement : } 11111111 \\ 2's \text{ complement : } 100000000 \end{array}$$

Problem: 1-18

Perform subtraction on the following unsigned binary numbers using the 2's-complement of the subtrahend. Where the result should be negative, 2's-complement it and affix a minus sign.

(a) 11011-11001 (b)110100 -10101 (c)1011-110000 (d)101010-101011

Solution:

a)

$$\begin{aligned}
 X &= 11011 & Y &= 11001 \\
 X &= & 11011 \\
 2's \text{ Complement of } Y &= + \underline{00111} \\
 Sum &= & 100010 \\
 \text{Discard end carry } 2^5 &= - \underline{100000} \\
 \text{Answer : } X - Y &= & 00010
 \end{aligned}$$

b)

$$\begin{aligned}
 X &= 110100 & Y &= 10101 \\
 X &= & 110100 \\
 2's \text{ Complement of } Y &= + \underline{101011} \\
 Sum &= & 1011111 \\
 \text{Discard end carry } 2^5 &= - \underline{1000000} \\
 \text{Answer : } X - Y &= & 011111
 \end{aligned}$$

c)

$$\begin{aligned}
 X &= 1011 & Y &= 110000 \\
 X &= & 1011 \\
 2's \text{ Complement of } Y &= + \underline{010000} \\
 Sum &= & 011011 \\
 \text{There is no end carry} \\
 \text{Answer : } Y - X &= - & 100101
 \end{aligned}$$

d)

$$\begin{aligned}
 X &= 101010 & Y &= 101011 \\
 X &= & 101010 \\
 2's \text{ Complement of } Y &= + \underline{010101} \\
 Sum &= & 111111 \\
 \text{There is no end carry} \\
 \text{Answer : } Y - X &= - & 000001
 \end{aligned}$$

Problem: 1-21

Convert decimal 9126 to both BCD and ASCII codes. For ASCII, an odd parity bit is to be appended at the left.

Solution:

$$(9126)_{10} = (1001\ 0001\ 0010\ 0110)_{BCD}$$

$$(9126)_{10} = (10111001\ 00110001\ 00110010\ 10110110)_{ASCII}$$

Problem: 1-31

What bit must be complemented to change an ASCII letter from capital to lowercase, and vice versa?

Solution:

To do so we complement b_6 .

Problem: 1-34

Assume a 3-input AND gate with output F and a 3-input OR gate with G output. Show the signals of the outputs F and G as functions of the three inputs ABC. Use all 8 possible combinations of ABC.

Solution: